System of Equations (No Solution)

1. Does each system of linear equations have a solution? Explain your answer.

a)
$$\begin{cases} y = \frac{5}{4}x - 3\\ y + 2 = \frac{5}{4}x \end{cases}$$

b)
$$\begin{cases} y = \frac{2}{3}x - 5\\ 4x - 8y = 11 \end{cases}$$

c)
$$\begin{cases} \frac{1}{3}x + y = 8\\ x + 3y = 12 \end{cases}$$

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a)
$$\begin{cases} y = \frac{5}{4}x - 3\\ y + 2 = \frac{5}{4}x \end{cases}$$

No, this system does not have a solution. The slope of the first equation is $\frac{5}{4}$, and the slope of the second equation is $\frac{5}{4}$. Since the slopes are the same, and they are distinct lines, these equations will graph as parallel lines. Parallel lines never intersect; therefore, this system has no solution.

b)
$$\begin{cases} y = \frac{2}{3}x - 5\\ 4x - 8y = 11 \end{cases}$$

Yes, this system does have a solution. The slope of the first equation is $\frac{2}{3}$, and the slope of the second equation is $\frac{1}{2}$. Since the slopes are different, these equations will graph as nonparallel lines, which means they will intersect at some point.

c)
$$\begin{cases} \frac{1}{3}x + y = 8\\ x + 3y = 12 \end{cases}$$

No, this system does not have a solution. The slope of the first equation is $-\frac{1}{3}$, and the slope of the second equation is $-\frac{1}{3}$. Since the slopes are the same, and they are distinct lines, these equations will graph as parallel lines. Parallel lines never intersect; therefore, this system has no solution.