

Using Radicals to Solve Equations

$$1. \ x^2(x + 7) = \frac{1}{2}(14x^2 + 16)$$

$$2. \ x^3 = 1331^{-1}$$

$$3. \ x^3 + 9x = \frac{1}{2}(18x + 54)$$

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$$1. \ x^2(x + 7) = \frac{1}{2}(14x^2 + 16)$$

Check:

$$\begin{aligned} x^2(x + 7) &= \frac{1}{2}(14x^2 + 16) \\ x^3 + 7x^2 &= 7x^2 + 8 \\ x^3 + 7x^2 - 7x^2 &= 7x^2 - 7x^2 + 8 \\ x^3 &= 8 \\ \sqrt[3]{x^3} &= \sqrt[3]{8} \\ x &= 2 \end{aligned}$$

$$\begin{aligned} 2^2(2 + 7) &= \frac{1}{2}(14(2^2) + 16) \\ 4(9) &= \frac{1}{2}(56 + 16) \\ 36 &= \frac{1}{2}(72) \\ 36 &= 36 \end{aligned}$$

$$2. \ x^3 = 1331^{-1}$$

$$\begin{aligned} x^3 &= 1331^{-1} \\ \sqrt[3]{x^3} &= \sqrt[3]{1331^{-1}} \\ x &= \sqrt[3]{\frac{1}{1331}} \\ x &= \sqrt[3]{\frac{1}{11^3}} \\ x &= \frac{1}{11} \end{aligned}$$

Check:

$$\begin{aligned} \left(\frac{1}{11}\right)^3 &= 1331^{-1} \\ \frac{1}{11^3} &= 1331^{-1} \\ \frac{1}{1331} &= 1331^{-1} \\ 1331^{-1} &= 1331^{-1} \end{aligned}$$

$$3. \ x^3 + 9x = \frac{1}{2}(18x + 54)$$

$$\begin{aligned} x^3 + 9x &= \frac{1}{2}(18x + 54) \\ x^3 + 9x &= 9x + 27 \\ x^3 + 9x - 9x &= 9x - 9x + 27 \\ x^3 &= 27 \\ \sqrt[3]{x^3} &= \sqrt[3]{27} \\ x &= \sqrt[3]{3^3} \\ x &= 3 \end{aligned}$$

$$\begin{aligned} 3^3 + 9(3) &= \frac{1}{2}(18(3) + 54) \\ 27 + 27 &= \frac{1}{2}(54 + 54) \\ 54 &= \frac{1}{2}(108) \\ 54 &= 54 \end{aligned}$$