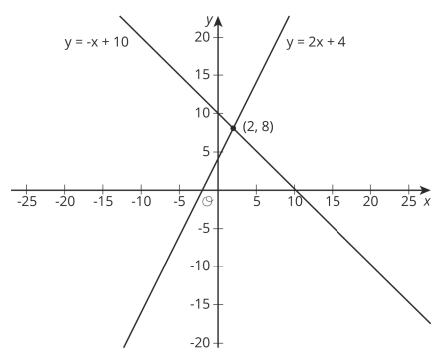
# Unit 4, Lesson 13: Solving Systems of Equations

Let's solve systems of equations.

#### 13.1: True or False: Two Lines



Use the lines to decide whether each statement is true or false. Be prepared to explain your reasoning using the lines.

- 1. A solution to 8 = -x + 10 is 2.
- 2. A solution to 2 = 2x + 4 is 8.
- 3. A solution to -x + 10 = 2x + 4 is 8.
- 4. A solution to -x + 10 = 2x + 4 is 2.
- 5. There are no values of x and y that make y = -x + 10 and y = 2x + 4 true at the same time.

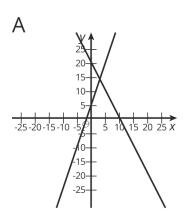


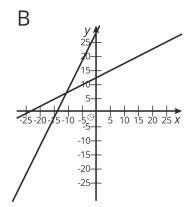
### 13.2: Matching Graphs to Systems

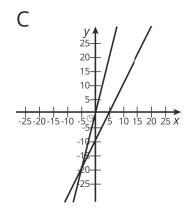
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Here are three **systems of equations** graphed on a coordinate plane:









1. Match each figure to one of the systems of equations shown here.

a. 
$$\begin{cases} y = 3x + 5 \\ y = -2x + 20 \end{cases}$$

b. 
$$\begin{cases} y = 2x - 10 \\ y = 4x - 1 \end{cases}$$

c. 
$$\begin{cases} y = 0.5x + 12 \\ y = 2x + 27 \end{cases}$$

2. Find the solution to each system and check that your solution is reasonable based on the graph.



#### 13.3: Different Types of Systems

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Your teacher will give you a page with some systems of equations.



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- 1. Graph each system of equations carefully on the provided coordinate plane.
- 2. Describe what the graph of a system of equations looks like when it has . . .
  - a. 1 solution
  - b. 0 solutions
  - c. infinitely many solutions

#### Are you ready for more?

The graphs of the equations Ax + By = 15 and Ax - By = 9 intersect at (2, 1). Find A and B. Show or explain your reasoning.

## **Lesson 13 Summary**

Sometimes it is easier to solve a system of equations without having to graph the equations and look for an intersection point. In general, whenever we are solving a system of equations written as

$$\begin{cases} y = [\text{some stuff}] \\ y = [\text{some other stuff}] \end{cases}$$

we know that we are looking for a pair of values (x, y) that makes both equations true. In particular, we know that the value for y will be the same in both equations. That means that

For example, look at this system of equations:

$$\begin{cases} y = 2x + 6 \\ y = -3x - 4 \end{cases}$$



Since the y value of the solution is the same in both equations, then we know

$$2x + 6 = -3x - 4$$

We can solve this equation for *x*:

$$2x + 6 = -3x - 4$$
  
 $5x + 6 = -4$  add  $3x$  to each side  
 $5x = -10$  subtract 6 from each side  
 $x = -2$  divide each side by 5

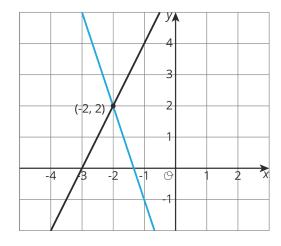
But this is only half of what we are looking for: we know the value for x, but we need the corresponding value for y. Since both equations have the same y value, we can use either equation to find the y-value:

$$y = 2(-2) + 6$$

Or

$$y = -3(-2) - 4$$

In both cases, we find that y = 2. So the solution to the system is (-2, 2). We can verify this by graphing both equations in the coordinate plane.

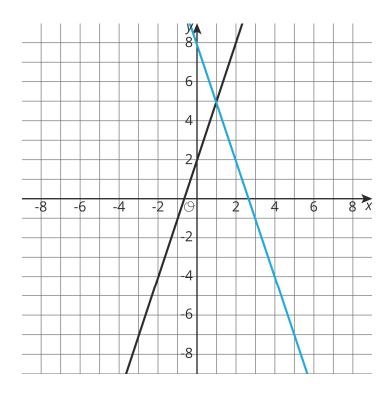


In general, a system of linear equations can have:

- No solutions. In this case, the lines that correspond to each equation never intersect.
- Exactly one solution. The lines that correspond to each equation intersect in exactly one point.
- An infinite number of solutions. The graphs of the two equations are the same line!

# **Unit 4, Lesson 13: Solving Systems of Equations**

1. a. Write equations for the lines shown.



- b. Describe how to find the solution to the corresponding system by looking at the graph.
- c. Describe how to find the solution to the corresponding system by using the equations.
- 2. The solution to a system of equations is (5, -19). Choose two equations that might make up the system.

A. 
$$y = -3x - 6$$

B. 
$$y = 2x - 23$$

C. 
$$y = -7x + 16$$

D. 
$$y = x - 17$$

E. 
$$y = -2x - 9$$

- 3. Solve the system of equations:  $\begin{cases} y = 4x 3 \\ y = -2x + 9 \end{cases}$
- 4. Solve the system of equations:  $\begin{cases} y = \frac{5}{4}x 2 \\ y = \frac{-1}{4}x + 19 \end{cases}$
- 5. Here is an equation:  $\frac{15(x-3)}{5} = 3(2x-3)$ 
  - a. Solve the equation by using the distributive property first.

b. Solve the equation without using the distributive property.

c. Check your solution.

(from Unit 4, Lesson 6)