Unit 2, Lesson 12: Using Equations for Lines

Let's write equations for lines.

12.1: Missing center

A dilation with scale factor 2 sends A to B. Where is the center of the dilation?
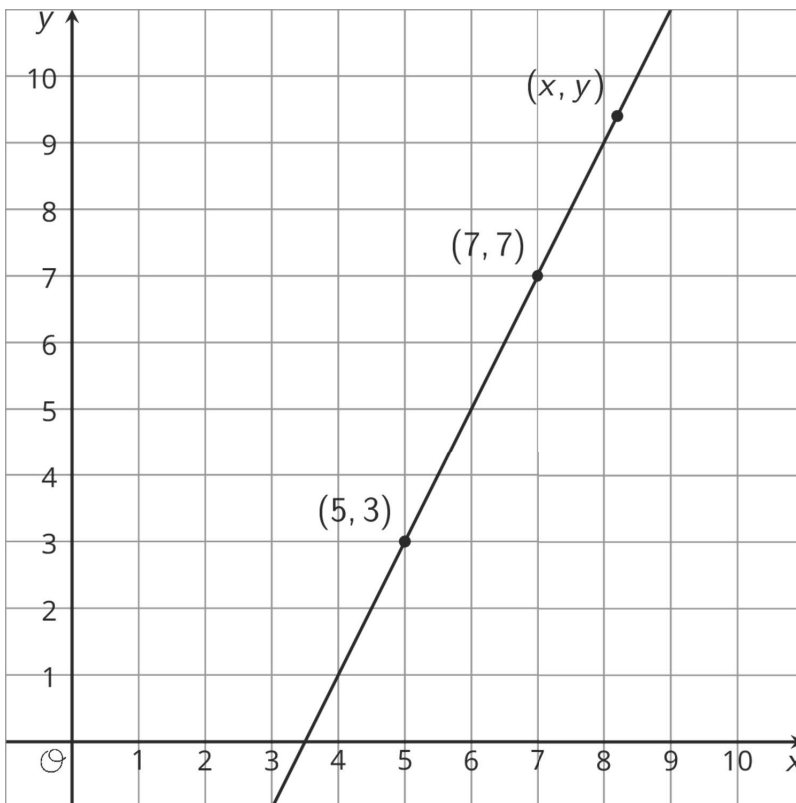
$\bullet B$

$\bullet A$

NAME   DATE   PERIOD

12.2: Writing Relationships from Two Points

Here is a line.

1. Using what you know about similar triangles, find an equation for the line in the diagram.

2. What is the slope of this line? Does it appear in your equation?

3. Is $(9, 11)$ also on the line? How do you know?

4. Is $(100, 193)$ also on the line?

Are you ready for more?

There are many different ways to write down an equation for a line like the one in the problem. Does $\frac{y-3}{x-6} = 2$ represent the line? What about $\frac{y-6}{x-4} = 5$? What about $\frac{y+5}{x-1} = 2$? Explain your reasoning.
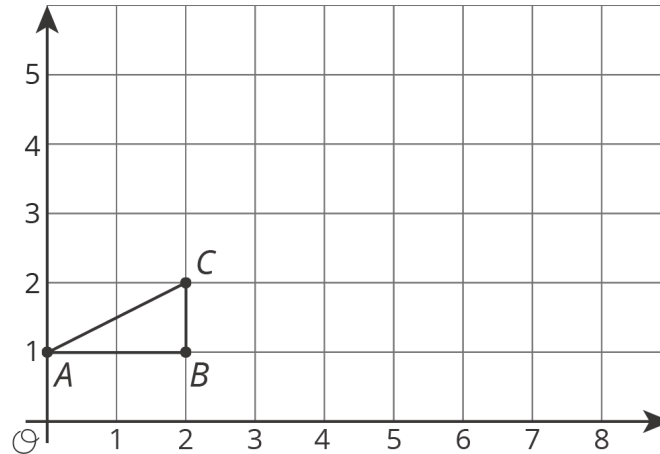
12.3: Dilations and Slope Triangles

Here is triangle ABC.

1. Draw the dilation of triangle ABC with center $(0, 1)$ and scale factor 2.

2. Draw the dilation of triangle ABC with center $(0, 1)$ and scale factor 2.5.

3. Where is C mapped by the dilation with center $(0, 1)$ and scale factor s?

4. For which scale factor does the dilation with center $(0, 1)$ send C to $(9, 5.5)$? Explain how you know.
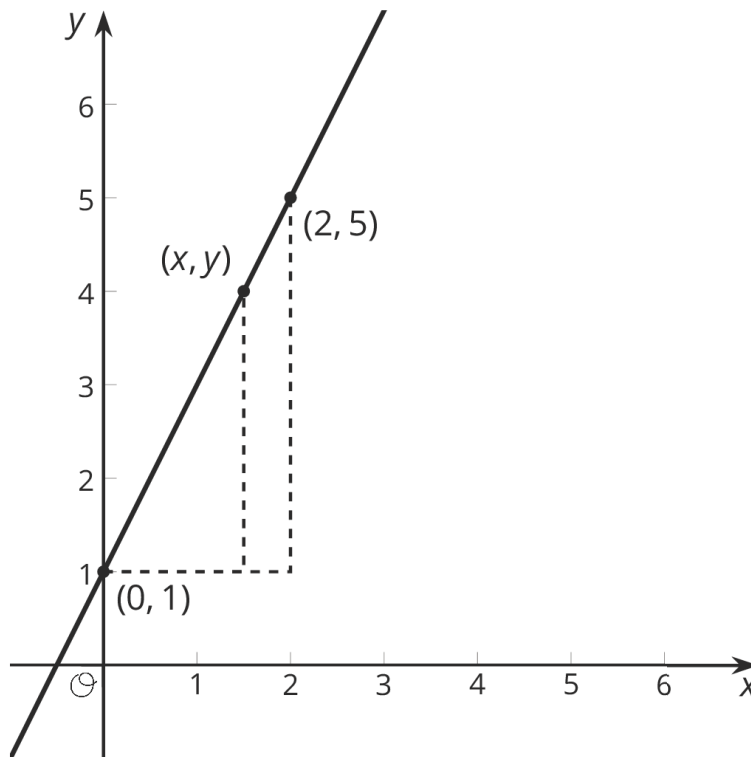
Lesson 12 Summary

We can use what we know about slope to decide if a point lies on a line. Here is a line with a few points labeled.

The slope triangle with vertices $(0, 1)$ and $(2, 5)$ gives a slope of $\frac{5-1}{2-0} = 2$. The slope triangle with vertices $(0, 1)$ and (x, y) gives a slope of $\frac{y-1}{x}$. Since these slopes are the same, $\frac{y-1}{x} = 2$ is an equation for the line. So, if we want to check whether or not the point $(11, 23)$ lies on this line, we can check that $\frac{23-1}{11} = 2$. Since $(11, 23)$ is a solution to the equation, it is on the line!

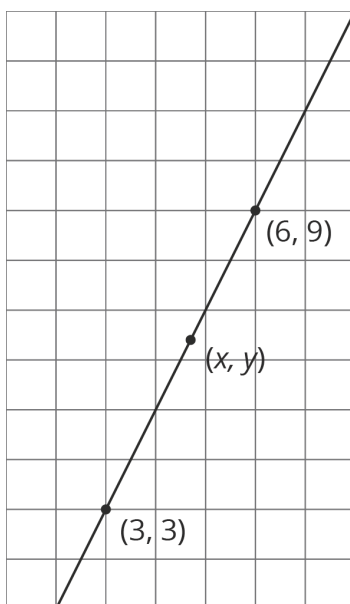NAME   DATE   PERIOD

Unit 2, Lesson 12: Using Equations for Lines

1. Select **all** the points that are on the line through $(0, 5)$ and $(2, 8)$.

   A. $(4, 11)$
   B. $(5, 10)$
   C. $(6, 14)$
   D. $(30, 50)$
   E. $(40, 60)$

2. All three points displayed are on the line. Find an equation relating x and y.
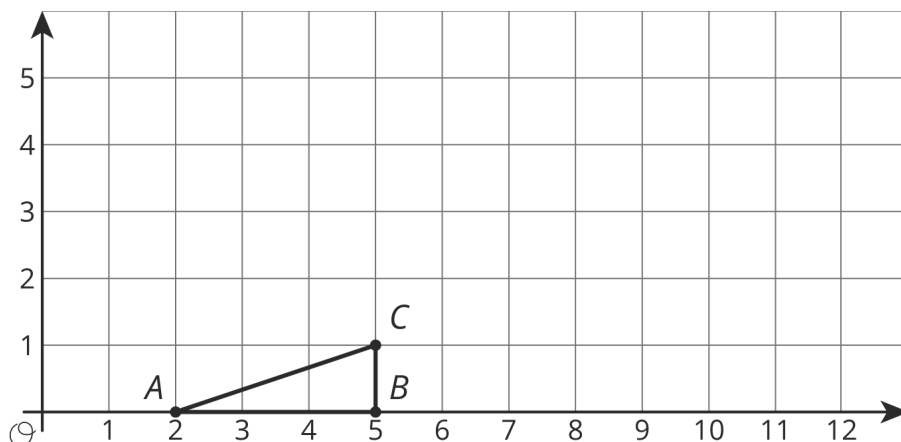

3. Here is triangle ABC.

NAME   DATE   PERIOD

a. Draw the dilation of triangle ABC with center $(2, 0)$ and scale factor 2.

b. Draw the dilation of triangle ABC with center $(2, 0)$ and scale factor 3.

c. Draw the dilation of triangle ABC with center $(2, 0)$ and scale factor $\frac{1}{2}$.

d. What are the coordinates of the image of point C when triangle ABC is dilated with center $(2, 0)$ and scale factor s?

e. Write an equation for the line containing all possible images of point C.

4. Here are some line segments.
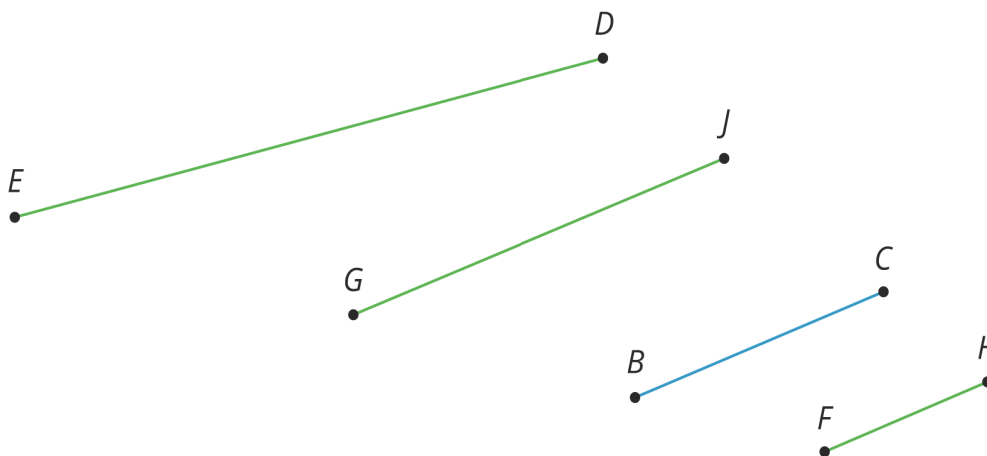
a. Which segment is a dilation of $\overline{BC}$ using A as the center of dilation and a scale factor of $\frac{2}{3}$?

b. Which segment is a dilation of $\overline{BC}$ using A as the center of dilation and a scale factor of $\frac{3}{2}$?

c. Which segment is not a dilation of $\overline{BC}$, and how do you know?

(from Unit 2, Lesson 4)