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Unit 1, Lesson 16: Parallel Lines and the Angles in a Triangle

Let's see why the angles in a triangle add to 180 degrees.

16.1: True or False: Computational Relationships

Is each equation true or false?

$$62 - 28 = 60 - 30$$

$$3 \cdot -8 = (2 \cdot -8) - 8$$

$$\frac{16}{-2} + \frac{24}{-2} = \frac{40}{-2}$$

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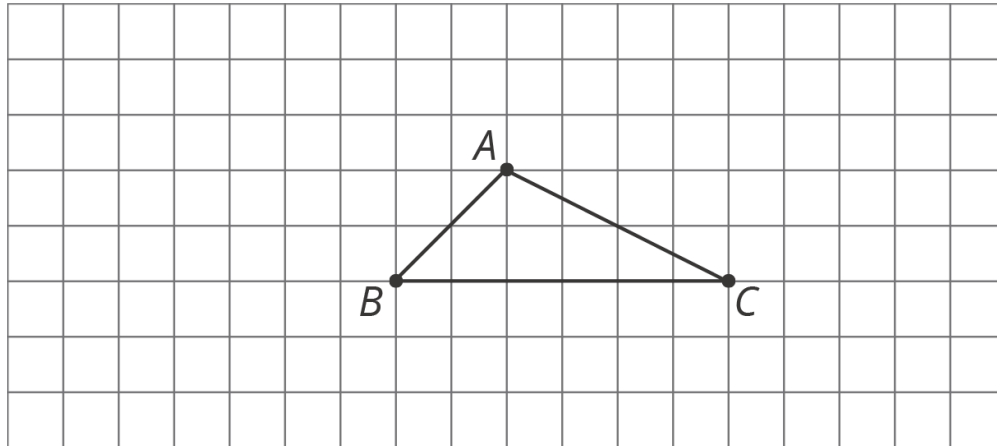
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16.2: Angle Plus Two

m.openup.org/1/8-1-16-2

Here is triangle ABC .



1. Rotate triangle ABC 180° around the midpoint of side AC . Label the new vertex D .
2. Rotate triangle ABC 180° around the midpoint of side AB . Label the new vertex E .
3. Look at angles EAB , BAC , and CAD . Without measuring, write what you think is the sum of the measures of these angles. Explain or show your reasoning.

4. Is the measure of angle EAB equal to the measure of any angle in triangle ABC ? If so, which one? If not, how do you know?

5. Is the measure of angle CAD equal to the measure of any angle in triangle ABC ? If so, which one? If not, how do you know?

6. What is the sum of the measures of angles ABC , BAC , and ACB ?

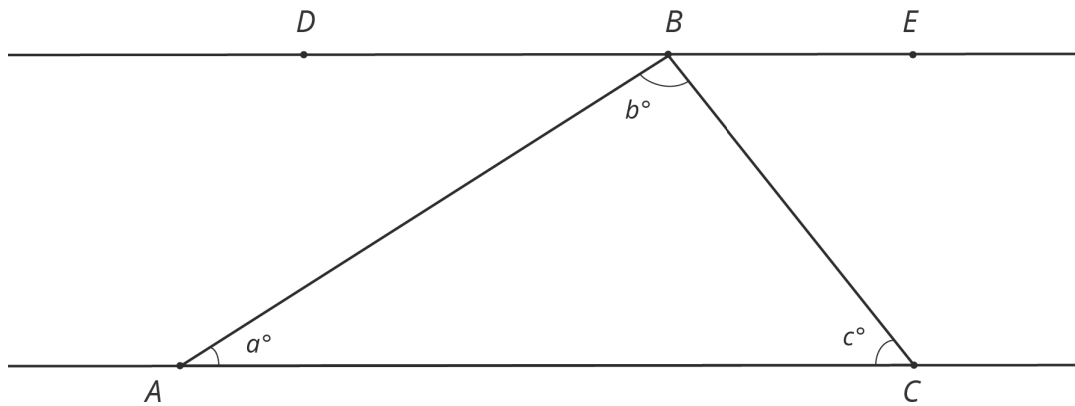
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16.3: Every Triangle in the World

Here is $\triangle ABC$. Line DE is parallel to line AC .



1. What is $m\angle DBA + b + m\angle CBE$? Explain how you know.
2. Use your answer to explain why $a + b + c = 180$.
3. Explain why your argument will work for *any* triangle: that is, explain why the sum of the angle measures in *any* triangle is 180° .

Are you ready for more?

1. Using a ruler, create a few quadrilaterals. Use a protractor to measure the four angles inside the quadrilateral. What is the sum of these four angle measures?
2. Come up with an explanation for why anything you notice must be true (hint: draw one diagonal in each quadrilateral).

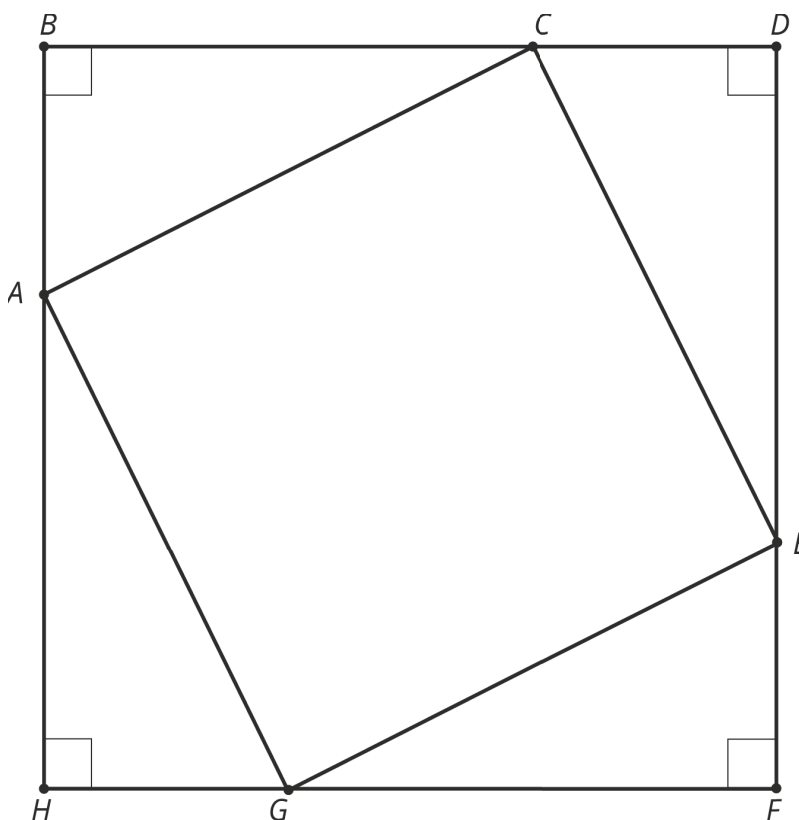
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16.4: Four Triangles Revisited

This diagram shows a square $BDFH$ that has been made by images of triangle ABC under rigid transformations.



Given that angle BAC measures 53 degrees, find as many other angle measures as you can.

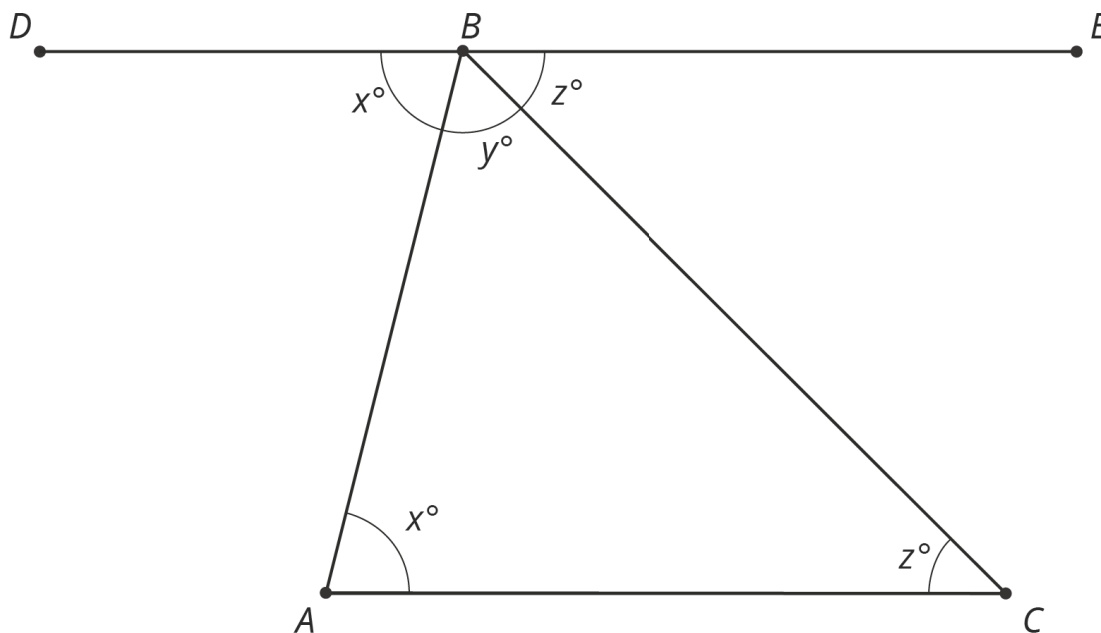
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Lesson 16 Summary

Using parallel lines and rotations, we can understand why the angles in a triangle always add to 180° . Here is triangle ABC . Line DE is parallel to AC and contains B .



A 180 degree rotation of triangle ABC around the midpoint of AB interchanges angles A and DBA so they have the same measure: in the picture these angles are marked as x° . A 180 degree rotation of triangle ABC around the midpoint of BC interchanges angles C and CBE so they have the same measure: in the picture, these angles are marked as z° . Also, DBE is a straight line because 180 degree rotations take lines to parallel lines. So the three angles with vertex B make a line and they add up to 180° ($x + y + z = 180$). But x, y, z are the measures of the three angles in $\triangle ABC$ so the sum of the angles in a triangle is always 180° !

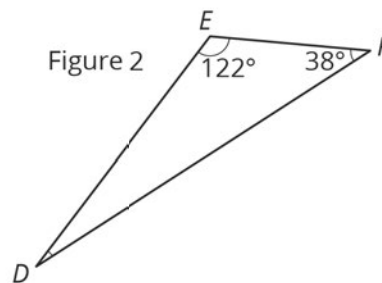
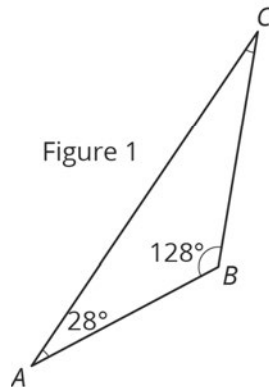
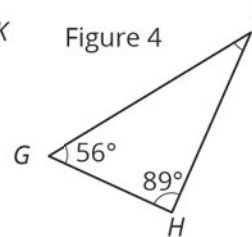
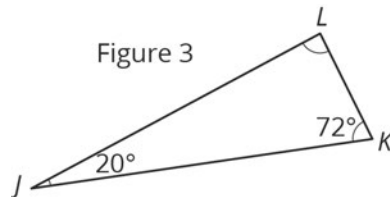
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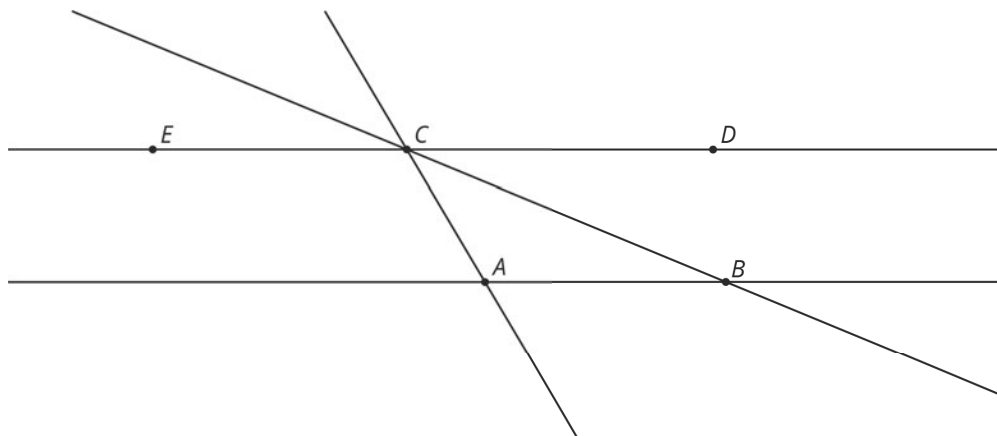
Unit 1, Lesson 16: Parallel Lines and the Angles in a Triangle

1. For each triangle, find the measure of the missing angle.



2. Is there a triangle with *two* right angles? Explain your reasoning.

3. In this diagram, lines AB and CD are parallel.



Angle ABC measures 35° and angle BAC measures 115° .

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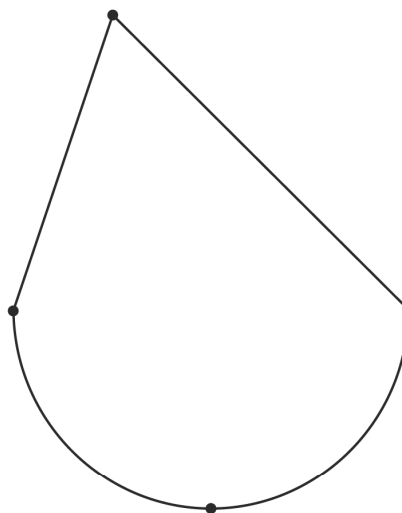
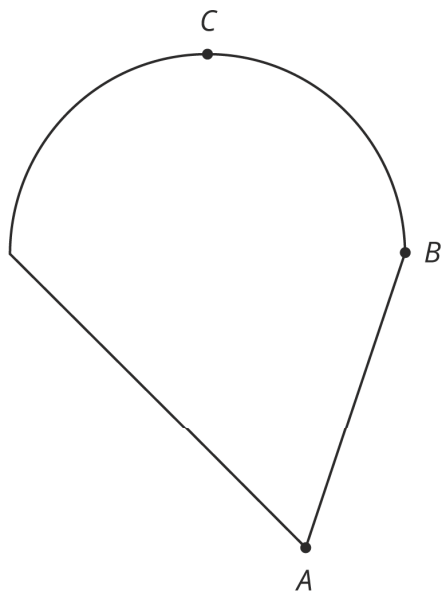
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- a. What is $m\angle ACE$?
- b. What is $m\angle DCB$?
- c. What is $m\angle ACB$?

4. The two figures are congruent.

- a. Label the points A' , B' and C' that correspond to A , B , and C in the figure on the right.

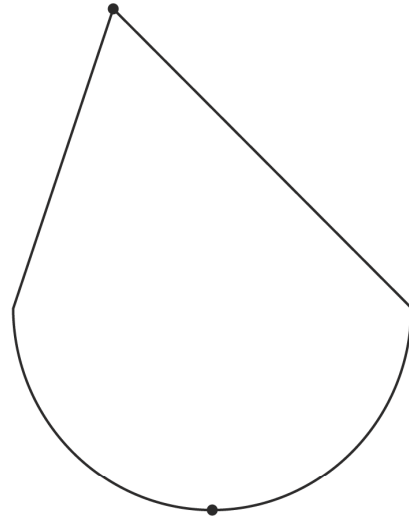
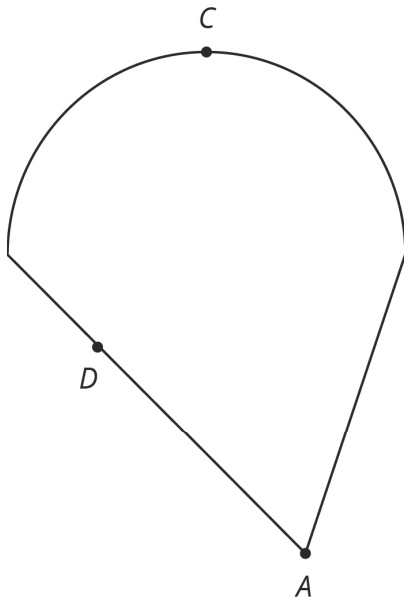


- b. If segment AB measures 2 cm, how long is segment $A'B'$? Explain.
- c. The point D is shown in addition to A and C . How can you find the point D' that corresponds to D ? Explain your reasoning.

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(from Unit 1, Lesson 13)