

Unit 4, Lesson 5: How Many Groups? (Part 2)

Let's use blocks and diagrams to understand more about division with fractions.

5.1: Reasoning with Fraction Strips

Write a fraction or whole number as an answer for each question. If you get stuck, use the fraction strips. Be prepared to share your strategy.

1. How many $\frac{1}{2}$ s are in 2?

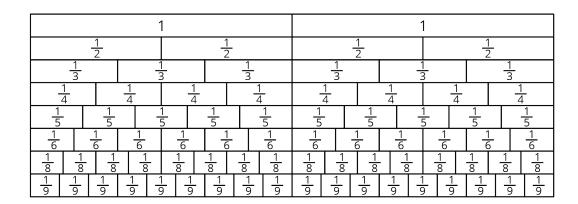
4. $1 \div \frac{2}{6} = ?$

2. How many $\frac{1}{5}$ s are in 3?

 $5.2 \div \frac{2}{9} = ?$

3. How many $\frac{1}{8}$ s are in $1\frac{1}{4}$?

 $6.4 \div \frac{2}{10} = ?$



5.2: More Reasoning with Pattern Blocks

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Your teacher will give you pattern blocks as shown here. Use them to answer the following questions.





- 1. If the trapezoid represents 1 whole, what do each of the following shapes represent? Be prepared to show or explain your reasoning.
 - a. 1 triangle

b. 1 rhombus

c. 1 hexagon

2. Use pattern blocks to represent each multiplication equation. Use the trapezoid to represent 1 whole.

a.
$$3 \cdot \frac{1}{3} = 1$$

b.
$$3 \cdot \frac{2}{3} = 2$$

- 3. Diego and Jada were asked "How many rhombuses are in a trapezoid?"
 - Diego says, " $1\frac{1}{3}$. If I put 1 rhombus on a trapezoid, the leftover shape is a triangle, which is $\frac{1}{3}$ of the trapezoid."
 - \circ Jada says, "I think it's $1\frac{1}{2}$. Since we want to find out 'how many rhombuses,' we should compare the leftover triangle to a rhombus. A triangle is $\frac{1}{2}$ of a rhombus."

Is the answer $1\frac{1}{3}$ or $1\frac{1}{2}$? Show or explain your reasoning.

4. Select **all** equations that can be used to answer the question: "How many rhombuses are in a trapezoid?"

a.
$$\frac{2}{3} \div ? = 1$$

c.
$$1 \div \frac{2}{3} = ?$$

e.
$$? \div \frac{2}{3} = 1$$

b.
$$? \cdot \frac{2}{3} = 1$$

d.
$$1 \cdot \frac{2}{3} = ?$$



5.3: Drawing Diagrams to Show Equal-sized Groups

For each situation, draw a diagram for the relationship of the quantities to help you answer the question. Then write a multiplication equation or a division equation for the relationship. Be prepared to share your reasoning.

1. The distance around a park is $\frac{3}{2}$ miles. Noah rode his bicycle around the park for a total of 3 miles. How many times around the park did he ride?

2. You need $\frac{3}{4}$ yard of ribbon for one gift box. You have 3 yards of ribbon. How many gift boxes do you have ribbon for?

3. The water hose fills a bucket at $\frac{1}{3}$ gallon per minute. How many minutes does it take to fill a 2-gallon bucket?

Are you ready for more?

How many heaping teaspoons are in a heaping tablespoon? How would the answer depend on the shape of the spoons?



Lesson 5 Summary

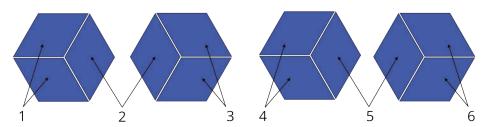
Suppose one batch of cookies requires $\frac{2}{3}$ cup flour. How many batches can be made with 4 cups of flour?

We can think of the question as being: "How many $\frac{2}{3}$ are in 4?" and represent it using multiplication and division equations.

$$? \cdot \frac{2}{3} = 4$$

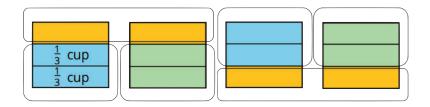
$$4 \div \frac{2}{3} = ?$$

Let's use pattern blocks to visualize the situation and say that a hexagon is 1 whole.



Since 3 rhombuses make a hexagon, 1 rhombus represents $\frac{1}{3}$ and 2 rhombuses represent $\frac{2}{3}$. We can see that 6 pairs of rhombuses make 4 hexagons, so there are 6 groups of $\frac{2}{3}$ in 4.

Other kinds of diagrams can also help us reason about equal-sized groups involving fractions. This example shows how we might reason about the same question from above: "How many $\frac{2}{3}$ -cups are in 4 cups?"



We can see each "cup" partitioned into thirds, and that there are 6 groups of $\frac{2}{3}$ -cup in 4 cups. In both diagrams, we see that the unknown value (or the "?" in the equations) is 6. So we can now write:

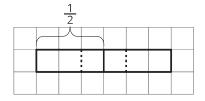
$$6 \cdot \frac{2}{3} = 4$$

$$4 \div \frac{2}{3} = 6$$

Unit 4, Lesson 5: How Many Groups? (Part 2)

1. Use the tape diagram to represent and find the value of $\frac{1}{2} \div \frac{1}{3}$.

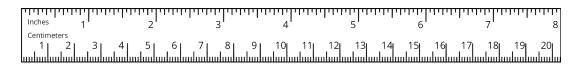
Mark up and label the diagram as needed.



2. What is the value of $\frac{1}{2} \div \frac{1}{3}$? Use pattern blocks to represent and find this value. The yellow hexagon represents 1 whole. Explain or show your reasoning.

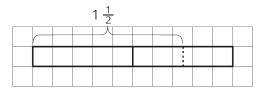


- 3. Use a standard inch ruler to answer each question. Then, write a multiplication equation and a division equation that answer the question.
 - a. How many $\frac{1}{2}$ s are in 7?
 - b. How many $\frac{3}{8}$ s are in 6?
 - c. How many $\frac{5}{16}$ s are in $1\frac{7}{8}$?



4. Use the tape diagram to represent and answer the question: How many $\frac{2}{5}$ s are in $1\frac{1}{2}$?

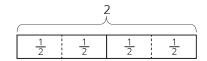
Mark up and label the diagram as needed.



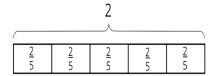
- 5. Write a multiplication equation and a division equation to represent each question, statement, or diagram.
 - a. There are 12 fourths in 3.

c. How many $\frac{2}{3}$ s are in 6?





d.



(from Unit 4, Lesson 4)

6. At a farmer's market, two vendors sell fresh milk. One vendor sells 2 liters for \$3.80, and another vendor sells 1.5 liters for \$2.70. Which is the better deal? Explain your reasoning.

(from Unit 3, Lesson 5)

- 7. A recipe uses 5 cups of flour for every 2 cups of sugar.
 - a. How much sugar is used for 1 cup of flour?
 - b. How much flour is used for 1 cup of sugar?
 - c. How much flour is used with 7 cups of sugar?
 - d. How much sugar is used with 6 cups of flour?

(from Unit 3, Lesson 6)