

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel
International
Advanced Level**

Centre Number

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Candidate Number

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Specimen Paper

(Time: 1 hour 30 minutes)

Paper Reference **WMA13/01**

Mathematics
International Advanced Level
Pure Mathematics P3

You must have:

Mathematical Formulae and Statistical Tables (Lilac), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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3. Guinea pigs and rabbits were introduced onto an island at the same time.

The number of guinea pigs, G , t months after they were introduced onto the island is modelled by the equation

$$G = a + 60e^{-0.05t}$$

where a is a positive constant.

The number of rabbits, R , t months after they were introduced onto the island is modelled by the equation

$$R = 100 + 80e^{0.05t}$$

Given that there were twice as many guinea pigs as rabbits introduced onto the island,

(a) find the value of a . (2)

When $t = T$, the number of rabbits on the island is equal to the number of guinea pigs on the island.

Using these models,

(b) find the value of T , giving your answer to one decimal place.
(Solutions based entirely on graphical or numerical methods are not acceptable.) (4)

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8. Liam monitored the population of a small country over a 10-year period.

The population, P , measured in thousands of people, is modelled by the equation

$$P = ab^{-t}$$

where a and b are constants and t is the number of years since monitoring began.

(a) Show that this equation can be expressed in the form

$$\log_{10} P = \log_{10} a - t \log_{10} b \tag{1}$$

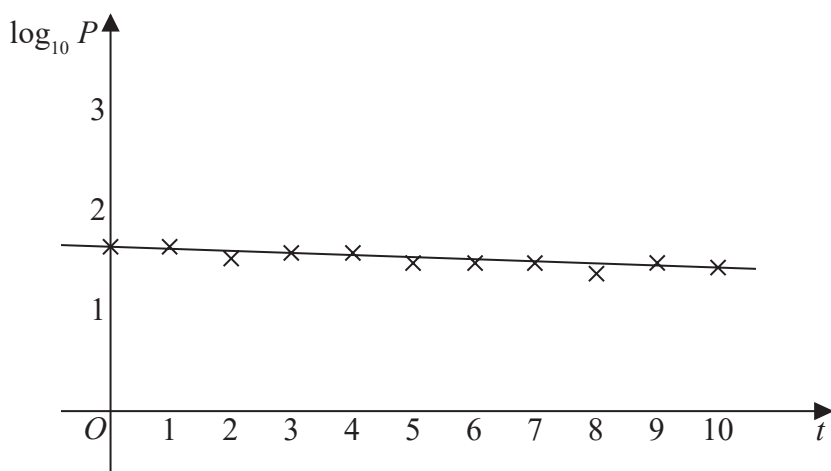


Figure 2

Figure 2 shows a line of best fit for values of t and $\log_{10} P$

The line of best fit passes through points $(0, 1.6)$ and $(10, 1.4)$

Using this information,

(b) find the value of a and the value of b , giving each answer to 4 significant figures. (4)

Hence, according to the model,

(c) find the rate at which the population was changing exactly 8 years after monitoring began. (3)

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10.

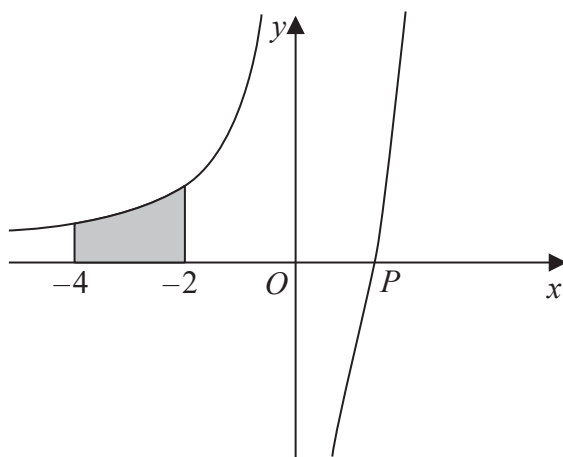


Figure 3

Figure 3 shows a sketch of the curve with equation

$$y = e^{2x-3} - \frac{4}{3x} \quad x \in \mathbb{R}, x \neq 0$$

The curve crosses the x -axis at the point $P(\alpha, 0)$.

(a) Show that

$$\alpha = \frac{1}{2} \left(\ln \left(\frac{4}{3\alpha} \right) + 3 \right) \tag{2}$$

The iteration formula

$$x_{n+1} = \frac{1}{2} \left(\ln \left(\frac{4}{3x_n} \right) + 3 \right)$$

is used to find an approximation to α .

(b) Taking $x_0 = 2$ find the value of x_1 and the value of x_5

Give each answer to 4 decimal places.

(2)

(c) Using a suitable interval and a suitable function that should be stated, show that to 3 decimal places α is 1.456

(2)

The finite region, shown shaded in Figure 3, is bounded by the curve, the line with equation $x = -4$, the x -axis and the line with equation $x = -2$

(d) Using integration find, in simplest form, the exact area of the shaded region.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(5)

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