

1. The graph of a function f is shown above. Which of the following statements about f is false?
- f is continuous at $x = a$.
 - f has a relative maximum at $x = a$.
 - $x = a$ is in the domain of f .
 - $\lim_{x \rightarrow a^+} f(x) = \lim_{x \rightarrow a^-} f(x)$.
 - $\lim_{x \rightarrow a} f(x)$ exists.

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2. For $x \geq 0$, the horizontal line $y = 2$ is an asymptote for the graph of the function f . Which of the following statements must be true?
- $f(0) = 2$
 - $f(x) \neq 2$ for all $x \geq 0$
 - $f(2)$ is undefined.
 - $\lim_{x \rightarrow 2} f(x) = \infty$
 - $\lim_{x \rightarrow \infty} f(x) = 2$

3. Let f be a function that is continuous on the closed interval $[2,4]$ with $f(2)=10$ and $f(4)=20$. Which of the following is guaranteed by the Intermediate Value Theorem?
- a. $f(x)=13$ has at least one solution in the open interval $(2,4)$.
 - b. $f(3)=15$.
 - c. f attains a maximum on the open interval $(2,4)$.
 - d. $f'(x)=5$ has at least one solution in the open interval $(2,4)$.
 - e. $f'(x)>0$ for all x in the open interval $(2,4)$.

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4. If $\lim_{x \rightarrow 3} f(x) = 7$, which of the following must be true?
- I. f is continuous at $x = 3$.
 - II. f is differentiable at $x = 3$.
 - III. $f(3) = 7$.
- a. None.
 - b. II only.
 - c. III only.
 - d. I and III only.
 - e. I, II, and III

5. If $\lim_{x \rightarrow a} f(x) = L$, where L is a real number, which of the following must be true?
- a. $f'(a)$ exists.
 - b. $f(x)$ is continuous at $x = a$.
 - c. $f(x)$ is defined at $x = a$.
 - d. $f(a) = L$
 - e. none of the above.

6. At $x = 3$, the function given by $f(x) = \begin{cases} x^2, & x < 3 \\ 6x - 9, & x \geq 3 \end{cases}$ is

- a. undefined.
- b. continuous but not differentiable.
- c. differentiable but not continuous.
- d. neither continuous nor differentiable.
- e. both continuous and differentiable.

7. Which of the following are continuous at $x = 1$?

I. $\ln(x)$

II. e^x

III. $\ln(e^x - 1)$

- a. I only
- b. II only
- c. I and II only
- d. II and III only
- e. I, II, and III

8. If the function f is continuous for all real numbers and if $f(x) = \frac{x^2 - 4}{x + 2}$ when $x \neq -2$, then $f(-2) =$

- a. -4
- b. -2
- c. -1
- d. 0
- e. 2

9. If f is a continuous function on $[a, b]$, which of the following is necessarily true?
- a. f' exists on (a, b) .
 - b. If $f(x_0)$ is a maximum of f , then $f'(x_0) = 0$.
 - c. $\lim_{x \rightarrow x_0} f(x) = f\left(\lim_{x \rightarrow x_0} x\right)$ for $x_0 \in (a, b)$.
 - d. $f'(x) = 0$ for some $x \in [a, b]$.
 - e. The graph of f' is a straight line.

$$f(x) = \begin{cases} \frac{x^2 - 4}{x - 2} & \text{if } x \neq 2 \\ 1 & \text{if } x = 2 \end{cases}$$

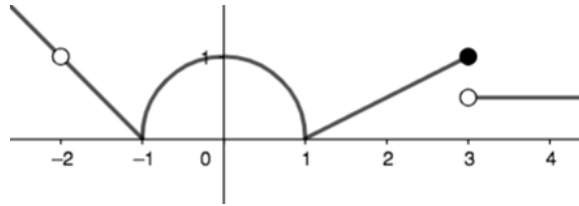
10. Let f be the function defined above. Which of the following statements about f are true?
- I. f has a limit at $x = 2$.
 - II. f is continuous at $x = 2$.
 - III. f is differentiable at $x = 2$.
- a. I only.
 - b. II only.
 - c. III only.
 - d. I and II only.
 - e. I, II, and III.

11. What is the domain of the function f given by $f(x) = \frac{\sqrt{x^2 - 4}}{x - 3}$?

- a. $\{x : x \neq 3\}$
 - b. $\{x : |x| \leq 2\}$
 - c. $\{x : |x| \geq 2\}$
 - d. $\{x : |x| \geq 2 \text{ and } x \neq 3\}$
 - e. $\{x : x \geq 2 \text{ and } x \neq 3\}$
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12. What is $\lim_{x \rightarrow \infty} \frac{x^2 - 4}{2 + x - 4x^2}$?

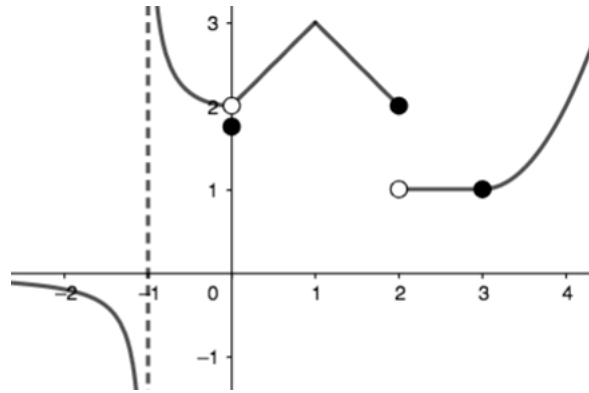
- a. -2
- b. $-\frac{1}{4}$
- c. $\frac{1}{2}$
- d. 1
- e. The limit does not exist.



13. The graph of a function f is shown above. For which of the following values of c does $\lim_{x \rightarrow c} f(x) = 1$?
- 0 only
 - 0 and 3 only
 - 2 and 0 only
 - 2 and 3 only
 - 2, 0, and 3

14. The graph of which of the following equations has $y = 1$ as an asymptote?

- $y = \ln(x)$
- $y = \sin(x)$
- $y = \frac{x}{x+1}$
- $y = \frac{x^2}{x+1}$
- $y = e^{-x}$



15. The graph of a function f is shown above. If $\lim_{x \rightarrow b} f(x)$ exists and f is not continuous at b , then $b =$

- a. -1
- b. 0
- c. 1
- d. 2
- e. 3

16. A polynomial $p(x)$ has a relative maximum at $(-2, 4)$, a relative minimum at $(1, 1)$, a relative maximum at $(5, 7)$, and no other critical points. How many zeros does $p(x)$ have?

- a. One
- b. Two
- c. Three
- d. Four
- e. Five

17. If a function f is continuous for all x and if f has a relative maximum at $(-1, 4)$ and a relative minimum at $(3, -2)$, which of the following statements must be true?
- a. The graph of f has a point of inflection somewhere between $x = -1$ and $x = 3$.
 - b. $f'(-1) = 0$
 - c. The graph of f has a horizontal asymptote.
 - d. The graph of f has a horizontal tangent at $x = 3$.
 - e. The graph of f intersects both axes.

18. Let f be a continuous function on the closed interval $[-3, 6]$. If $f(-3) = -1$ and $f(6) = 3$, then the Intermediate Value Theorem guarantees that

- a. $f(0) = 0$
- b. $f'(c) = \frac{4}{9}$ for at least one c between -3 and 6 .
- c. $-1 \leq f(x) \leq 3$ for all x between -3 and 6 .
- d. $f(c) = 1$ for at least one c between -3 and 6 .
- e. $f(c) = 0$ for at least one c between -1 and 3 .

x	0	1	2
$f(x)$	1	k	2

19. The function f is continuous on the closed interval $[0,2]$ and has values that are given in the table

above. The equation $f(x) = \frac{1}{2}$ must have at least two solutions in the interval $[0,2]$ if $k =$

- a. 0
- b. $\frac{1}{2}$
- c. 1
- d. 2
- e. 3

20. Let f be a function that is differentiable on the open interval $(1,10)$. If $f(2) = -5$, $f(5) = 5$, and $f(9) = -5$, which of the following must be true?

- I. f has at least 2 zeros.
- II. The graph of f has at least one horizontal tangent.
- III. For some c , $2 < c < 5$, $f(c) = 3$.

- a. None
- b. I only
- c. I and II only
- d. I and III only
- e. I, II, and III

21. Let g be a continuous function on the closed interval $[0,1]$. Let $g(0)=1$ and $g(1)=0$. Which of the following is NOT necessarily true?
- a. There exists a number h in $[0,1]$ such that $g(h) \geq g(x)$ for all x in $[0,1]$.
 - b. For all a and b in $[0,1]$, if $a = b$, then $g(a) = g(b)$.
 - c. There exists a number h in $[0,1]$ such that $g(h) = \frac{1}{2}$.
 - d. There exists a number h in $[0,1]$ such that $g(h) = \frac{3}{2}$.
 - e. For all h in the open interval $(0,1)$, $\lim_{x \rightarrow h} g(x) = g(h)$.

22. $\lim_{x \rightarrow 0} \frac{5x^4 + 8x^2}{3x^4 - 16x^2}$ is

- a. $-\frac{1}{2}$
- b. 0
- c. 1
- d. $\frac{5}{3}$
- e. nonexistent

23. $\lim_{x \rightarrow \infty} \frac{(2x-1)(3-x)}{(x-1)(x+3)}$ is

- a. -3
- b. -2
- c. 2
- d. 3
- e. nonexistent

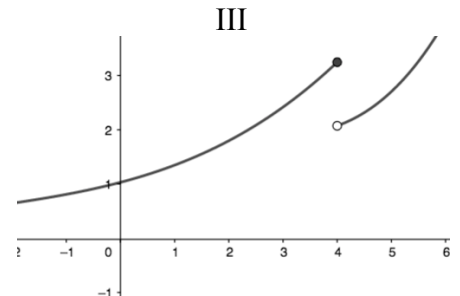
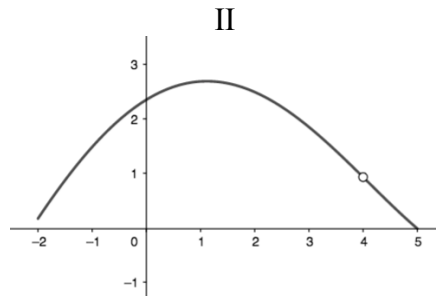
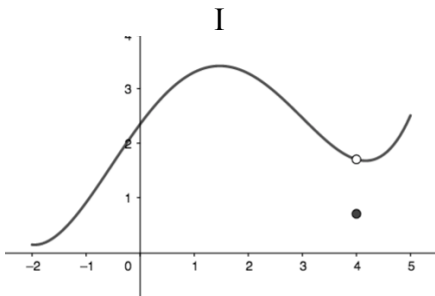
24. $\lim_{x \rightarrow \infty} \frac{x^3 - 2x^2 + 3x - 4}{4x^3 - 3x^2 + 2x - 1}$ is

- a. 4
- b. 1
- c. $\frac{1}{4}$
- d. 0
- e. -1

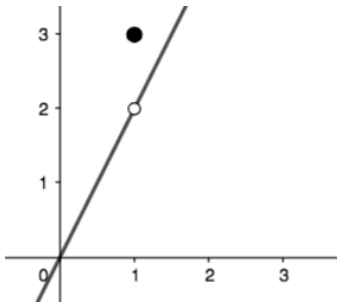
25. $\lim_{n \rightarrow \infty} \frac{3n^3 - 5n}{n^3 - 2n^2 + 1}$ is

- a. -5
- b. -2
- c. 1
- d. 3
- e. nonexistent

26. For which of the following does $\lim_{x \rightarrow 4} f(x)$ exist?



- a. I only
- b. II only
- c. III only
- d. I and II only
- e. I and III only

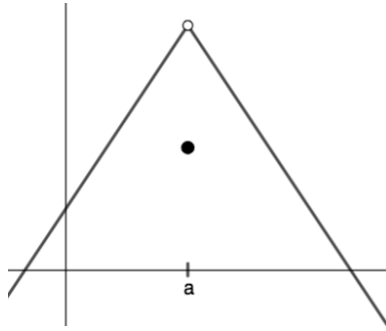


27. The graph of the function f is shown in the figure above. The value of $\lim_{x \rightarrow 1} (\sin(f(x)))$ is

- a. 0.909
- b. 0.841
- c. 0.141
- d. -0.416
- e. nonexistent

28. If $f(x) = \begin{cases} \ln(x) & \text{for } 0 < x \leq 2 \\ x^2 \ln(2) & \text{for } 2 < x \leq 4 \end{cases}$, then $\lim_{x \rightarrow 2} f(x)$ is

- a. $\ln(2)$
- b. $\ln(8)$
- c. $\ln(16)$
- d. 4
- e. nonexistent

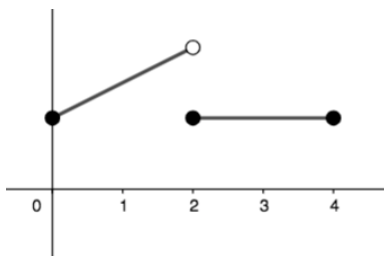


29. The graph of the function f is shown above. Which of the following statements must be false?

- a. $f(a)$ exists
- b. $f(x)$ is defined for $0 < x < a$.
- c. f is not continuous at $x = a$.
- d. $\lim_{x \rightarrow a} f(x)$ exists.
- e. $\lim_{x \rightarrow a} f'(x)$ exists.

30. If $a \neq 0$, then $\lim_{x \rightarrow a} \frac{x^2 - a^2}{x^4 - a^4}$ is

- a. $\frac{1}{a^2}$
- b. $\frac{1}{2a^2}$
- c. $\frac{1}{6a^2}$
- d. 0
- e. nonexistent



31. The figure above shows the graph of a function f with domain $0 \leq x \leq 4$. Which of the following statements are true?

- I. $\lim_{x \rightarrow 2^-} f(x)$ exists.
- II. $\lim_{x \rightarrow 2^+} f(x)$ exists.
- III. $\lim_{x \rightarrow 2} f(x)$ exists.

- a. I only
- b. II only
- c. I and II only
- d. I and III only
- e. I, II, and III

$$f(x) = \begin{cases} \frac{(2x+1)(x-2)}{(x-2)} & \text{for } x \neq 2 \\ k & \text{for } x = 2 \end{cases}$$

32. Let f be the function defined above. For what value of k is f continuous at $x = 2$?

- a. 0
- b. 1
- c. 2
- d. 3
- e. 5

33. If the graph of $y = \frac{ax+b}{x+c}$ has a horizontal asymptote $y = 2$ and a vertical asymptote $x = -3$, then

$$a + c =$$

- a. -5
- b. -1
- c. 0
- d. 1
- e. 5